

LESSON 7 – APPLICATION EXERCISE 1**(Bring a 3.5" computer disk to class)***We'll use an Excel spreadsheet to model horizontal and vertical fights. Which fighter will win?***Reading:****"The Problem of the Pullout" Handout****Problems/Questions:**

Work on Problem Set 2

Objectives:

7-1 Understand how Euler's method can be used to model aircraft performance.

7-2 Be able to compare an aircraft's performance in a level turn versus a vertical turn.

LESSON 8 – APPLICATION EXERCISE 1 CONTINUED**(Bring a 3.5" computer disk to class)***OK, so modeling something this complex isn't that quick and easy. You'll now get a chance to finish up your first application exercise.***Reading:****"The Problem of the Pullout" Handout****Problems/Questions:**

Work on Problem Set 2 and Application Exercise 1

Objectives:

8-1 Understand how Euler's method can be used to model aircraft performance.

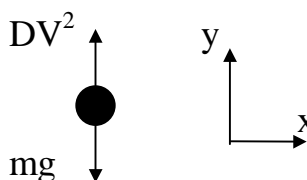
8-2 Be able to compare an aircraft's performance in a level turn versus a vertical turn.

Last Time: Entering and leaving a turning fight
 Last-Ditch Options
 Flat/Rolling Scissors
 Neutral Low-Aspect BFM

Today: Modeling a level turn (7); Modeling a vertical turn (8)

Equations: See last page of these notes

Discuss the Euler method of iterative calculation. Use an example of a ball dropping in a resistive medium.



$$\begin{aligned}\Sigma F_y &= ma_y \\ -mg + DV^2 &= ma_y \\ a_y &= -g + DV^2/m\end{aligned}$$

For this simple case, let $D = 1 \text{ kg/m}$, $m = 1 \text{ kg}$, and $g = 10 \text{ m/s}^2$.

From kinematics, $y = y_0 + v_{y0}\Delta t + \frac{1}{2} a_y(\Delta t)^2$, but Δt is small so $(\Delta t)^2$ is negligible and the position equation becomes $y = y_0 + v_{y0}\Delta t$. The velocity equation is simply $v = v_0 + a_y\Delta t$, and the acceleration equation comes from the free body diagram. To solve this, we only need two initial conditions: the position and velocity at time $t = 0$.

Step	Time	Position	Velocity	Acceleration
0	0.0	0	0	$-g + DV_0^2/m = -10+0=-10$
1	0.1	$y_0 + v_{y0}\Delta t = 0+0=0$	$v_0 + a_{y0}\Delta t = 0+(-10)(0.1)=-1$	$-g + DV_1^2/m = -10+(1)(1)/(1)=-9$
2	0.2	$y_1 + v_{y1}\Delta t = 0+(-1)(.1)=-.1$	$v_1 + a_{y1}\Delta t = -1+(-9)(.1)=-1.9$	$-g + DV_2^2/m = -10+(1)(3.61)/1=-6.39$
n	$n(\Delta T)$	$y_{n-1} + v_{yn-1}\Delta t$	$v_{n-1} + a_{yn-1}\Delta t$	$-g + DV_n^2/m$

Show “Level Turn.xls” on the screen. Discuss the blocks and how the specific excess energy is calculated.

PUT THESE UNIT CONVERSIONS ON THE BOARD:

$$\begin{aligned}
 1\text{kt} &= 0.51479 \text{ m/s} & 1\text{m} &= 3.28\text{ft} & g &= 9.81 \text{ m/s}^2 \\
 \text{timestep} &= 0.1\text{s} & 1\text{NM} &= 6076\text{ft} & 1\text{hr} &= 3600\text{s} \\
 \text{Speed of sound at 10,000 ft} &= 328.7 \text{ m/s}
 \end{aligned}$$

Formulae for level turn:

$$\text{Time} = (\text{oldtime}) + (\text{timestep})$$

$$\text{Airspeed} = (\text{old airspeed}) + (\text{timestep})(\text{acceleration})$$

$$\text{Mach} = (\text{airspeed})(\text{m/s to kt conversion})(\text{mach}/328.7 \text{ m/s})$$

$$\text{Rate} = (\text{load})(g)(\text{deg/rad conversion})/[(\text{airspeed})(\text{kt to m/s conversion})]$$

$$\text{Avg Rate} = (\text{Angle})/(\text{time})$$

$$\text{Angle} = (\text{old angle}) + (\text{timestep})(\text{rate})$$

$$\text{Radius} = [(\text{airspeed})(\text{m/s to kt conversion})]^2(\text{ft to m conversion})/[(\text{load})(g)]$$

$$\text{Acceleration} = (g)(\text{Ps})(\text{sec to hr conversion})/[(\text{airspeed})(\text{m/s to kt conversion})(\text{ft to NM conversion})]$$

$$\text{Specific energy} = (\text{airspeed})^2[(\text{m/s to kt conversion})^2(2g)^{-1}(\text{ft to m conversion})] + \text{altitude}$$